Introductory mathematical course

Introductory mathematical course in calculus for students of IT, engineering, economics etc.

Teaching and learning strategies implemented: Flipped classroom (FC), Instruction-based learning and Project-based learning (PBL-WBL)

Planned ECTS: 5, Number of learners: 200, Mode of delivery: Blended

Status: IN PLANNING, Course public access: Public

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Course learning outcome	Level	Weight
Explain the concept of the derivative of a real function of one real variable and its geometric interpretation	Understanding	10
Analyze an elementary function using derivatives and sketch its graph	Analysing	12
Apply differential calculus to find local extrema of a function with one variable and inflection points of the function.	Applying	12
Determine the primitive function and apply integral calculus in calculating surface area and volume.	Applying	12
Analyze and solve a problem task in the area of mathematical analysis of the function of one variables	Analysing	10
Create a program solution for a specific mathematical problem and present the solution in written format	Creating	16
Explain the concept of primitive function and integrals of a function with one variable	Understanding	10
Define elementary functions of a real variable, analyze their properties and sketch their graphs.	Analysing	10
Explain a concept of a limit and determine standard limits of functions	Applying	8

Topic / Unit name	Workload		Mode of	f delivery		Groups	Collaboration	Feedback	Assess	ment	
		type							Points	Types	Providers
Introduction											
Introduction of the cou	rse and TL	-As									
Introduction of the course Content, assessment and TLAs	45 min	Acquisition	Hybrid	Synchronous	Teacher present	No	No	No	No		
Disscusssion Students use disscusion online and ask questions, propose ideas	60 min	Discussion	Hybrid	Asynchronous	Teacher not present	No	Yes	Peer	No		
Total unit workload	1 75h										

	Workload		Mode of delivery	Groups	Collaboration	Feedback	Assessi	ment	
name		type					Points	Types	Providers

Real functions of real variables

Analyze and solve a problem task in the area of mathematical analysis of the function of one variables (40%), Define elementary functions of a real variable, analyze their properties and sketch their graphs. (60%)

The domain of the function. Composition. Bijection. Graph of the function.

Repetition of basic concepts	30 min	Acquisition	Online	Asynchronous	Teacher not present	No	No	No	No
Students					present				
receive a pre-									
prepared									
video with									
which they									
repeat basic									
concepts of									
function and									
graphs of									
elementary									
functions.									

Disscusion Students participate in discussions related to the introductory video. They can ask questions that can be answered by other students or a teacher.	15 min	Discussion	Online	Asynchronous	Teacher	No	No	Peer, Teacher	No		
Quiz (basic concepts) Students take a short quiz which cover the basic notions from the video.	10 min	Assessment	Online	Asynchronous	Teacher not present	No	No	Automated	1	Summative	Automated

Lecture	120 min	Acquisition	Hybrid	Synchronous	Teacher	No	No	No	No
Professor					present				
checks how									
many									
students									
watched the									
video lesson									
and what the									
quiz results									
were. Based									
on the results									
of the quiz,									
teacher									
repeats									
concepts that									
are less well									
understood									
and designs									
lecture to									
upgrade and									
broad the									
topic.									
Students									
have									
possibility for									
additional									
questions.									

Practice Assistants work with students. During the exercises, students do standard tasks related to the topic. In a group, they solve slightly more complex tasks.	90 min	Practice	Hybrid	Synchronous	Teacher	Yes	No	Teacher, Peer	No
Total unit workload	4.41h								
Properties of re	eal function	ns of a real v	variable						
Properties of real functions Students receive a preprepared video with which they repeat basic properties of	30 min	Acquisition	Online	Asynchronous	Teacher not present	No	No	No	No

real functions.

Disscusion Students participate in discussions related to the introductory video. They can ask questions that can be answered by other students or a teacher.	15 min	Discussion	Online	Asynchronous	Teacher	No	No	Peer	No		
Quiz (properties of real function) Students take a short quiz which cover the basic notions from the video.	10 min	Assessment	Online	Asynchronous	Teacher not present	No	No	Automated	1	Summative	Automated

Lecture Professor	120 min	Acquisition	Hybrid	Synchronous	Teacher present	No	No	No	No
checks how									
many									
students									
watched the									
video lesson									
and what the									
quiz results									
were. Based									
on the results									
of the quiz,									
teacher									
repeats									
concepts that									
are less well									
understood									
and designs									
lecture to									
upgrade and									
broad the									
topic.									
Students									
have									
possibility for									
additional									
questions.									

Practice Assistants work with students. During the exercises, students do standard tasks related to the topic. In a group, they solve slightly more complex tasks.	90 min	Practice	Hybrid	Synchronous	Teacher	Yes	No	Teacher, Peer	No		
Independent practical work Students work independently using the material in LMS Moodle and textbook.	90 min	Practice	Onsite	Asynchronous	Teacher not present	No	Yes	Automated, Peer	No		
Quiz (properties of real functionmath problems) Students take a short quiz which cover the basic math problems.	30 min	Assessment	Online	Asynchronous	Teacher not present	No	No	Automated	2	Summative	Automated

Total unit 6.41h workload

Examples of functions and their graphs

Examples (real functions of real variable) Students receive a pre- prepared video with which they repeat basic properties of real functions.	30 min	Acquisition	Online	Asynchronous	Teacher not present	No	No	No	No		
Disscusion Students participate in discussions related to the introductory video.	15 min	Discussion	Online	Asynchronous	Teacher present	No	No	Peer, Teacher	No		
Quiz (examples) Students take a short quiz which cover the basic notions from the video.	10 min	Assessment	Online	Asynchronous	Teacher not present	No	No	Automated	1	Summative	Automated

Lecture	120 min	Acquisition	Hybrid	Synchronous	Teacher	No	No	No	No
Professor					present				
checks how									
many									
students									
watched the									
video lesson									
and what the									
quiz results									
were. Based									
on the results									
of the quiz,									
teacher									
repeats									
concepts that									
are less well									
understood									
and designs									
lecture to									
upgrade and									
broad the									
topic.									
Students									
have									
possibility for									
additional									
questions.									

Practice Assistants work with students. During the exercises, students do standard tasks related to the topic. In a group, they solve slightly more complex tasks.	90 min	Practice	Hybrid	Synchronous	Teacher	Yes	No	Teacher, Peer	No
Independent practical work Students work independently using the material in LMS Moodle and textbook.	90 min	Practice	Onsite	Asynchronous	Teacher not present	No	Yes	Automated, Peer	No
Total unit workload	5.91h								

Sequences of real numbers and their properties

Examples (real functions	90 min	Investigation	Online	Asynchronous	Teacher not	No	No	No	No
of real					present				
variable)									
Students									
receive a pre-									
prepared									
materials with									
which they									
repeat basic									
properties of									
sequences.									
Students									
have to									
independently									
investigate									
and repeat									
the basic									
concepts of									
arithmetic									
and									
geometric									
series.									

Lecture	180 min	Acquisition	Hybrid	Synchronous	Teacher	No	No	No	No		
Teacher					present						
repeats basic											
concepts of											
sequences											
(definition,											
arithmetic											
and											
geometric											
sequences,											
properties											
and examples											
of sequences)											
and upgrades											
and broad the											
topic with											
limit of											
sequence.											
Quiz	10 min	Assessment	Online	Asynchronous	Teacher	No	No	Automated	1	Summative	Automated
(sequences)					not						
Students take					present						
a short quiz											
which cover											
the basic											
notions from											
lecture.											

Practice Assistants work with students. During the exercises, students do standard tasks related to the topic. In a group, they solve slightly more complex tasks.	180 min	Practice	Hybrid	Synchronous	Teacher	Yes	No	Teacher, Peer	No		
Independent practical work Students work independently using the material in LMS Moodle and textbook.	120 min	Practice	Onsite	Asynchronous	Teacher not present	No	Yes	Automated, Peer	No		
Quiz (sequences- math problems) Students take a short quiz which cover basic math problems.	30 min	Assessment	Online	Asynchronous	Teacher not present	No	No	Automated	2	Summative	Automate
Total unit workload	10.16h										

Topic / Unit name	Workload		Mode of delivery	Groups	Collaboration	Feedback	Assessi	ment	
		type					Points	Types	Providers

Limit of functions

Explain a concept of a limit and determine standard limits of functions (100%), Analyze an elementary function using derivatives and sketch its graph (10%), Define elementary functions of a real variable, analyze their properties and sketch their graphs. (10%)

Limit of function

Motivational example	60 min	Acquisition	Online	Asynchronous	Teacher not	No	No	No	No
Students					present				
receive a pre-									
prepared video									
with									
motivational									
example for									
limit of									
function and									
intuitive									
definition.									

Lecture Professor	180 min	Acquisition	Hybrid	Synchronous	Teacher present	No	No	No	No		
checks how											
many students											
watched the											
video lesson.											
Professor											
explains basic											
concepts and											
designs lecture											
to upgrade and											
broad the topic											
(Heine's and											
Cauchy's											
definition of											
function limit,											
main											
properties and											
theorems with											
proofs,											
continuity of											
function).											
Students have											
possibility for											
additional											
questions.											
Quiz (limit of function)	15 min	Assessment	Online	Asynchronous	Teacher	No	No	Automated	1	Summative	Automated
Students take					present						
a short quiz					present						
which cover											
the basic											
notions from											
lecture.											
icciule.											

Practice Assistants work with students. During the exercises, students do standard tasks related to the topic. In a group, they solve slightly more complex tasks.	120 min	Practice	Hybrid	Synchronous	Teacher	No	No	No	No		
Independent practical work Students work independently using the material in LMS Moodle and textbook.	180 min	Practice	Onsite	Asynchronous	Teacher not present	No	Yes	Automated, Peer	No		
Quiz (limit of function-math problems) Students take a short quiz which cover the basic math problems.	60 min	Assessment	Online	Asynchronous	Teacher not present	No	No	Automated	2	Summative	Automated
Total unit workload	10.25h										

Topic / Unit name	Workload		Mode of	f delivery	Gro	ıps (Collaboration	Feedback	Assessi	ment	
		type							Points	Types	Providers
Monthly test	1										
Analyze and solve	a problem ta	ask in the area	of mathe	ematical analysis	of the function	of on	ne variables (1	0%) , Define e	elementa	ry function	ns of a real
/ariable, analyze t	heir properti	es and sketch	their grap	ohs. (20%)							
	11 1 1										
reparation fot	tne test										
Independent practical work Students work independently	200 min	Practice	Onsite	Asynchronous	Teacher No not present	١	Yes	Automated, Peer	No		

not

present

Peer

Total unit 4.33h workload

about technical

related isssues Students are

information in LMS and then they can ask questions.

and content

given

Monthly test (kolokvij)

Test The test is	90 min	Assessment	Hybrid	Synchronous	Teacher present	No	No	Teacher, Automated	20	Formative	Teacher, Automated
prepared in											
hybrid delivery											
mode using											
individualised											
assignments											
from the											
databases in											
LMS.											
Total unit	1.5h										

Total unit workload

1.5h

Analysis of the test

Students' feedback A questionnaire with open and closed questions is used. Students give feedback to teachers (technical and	20 min	Discussion	Online	Asynchronous	Teacher not present	No	No	No	No
Analysis of the test Reliability, validity, students' satisfaction survey, explaining solutions	45 min	Discussion	Hybrid	Synchronous	Teacher	No	No	Teacher	No

Further student investigation	90 min	Investigation	Online	Asynchronous	Teacher not	Yes	Yes	Peer	No
Students investigate application areas of mathematics learned.					present				
Total unit workload	2.58h								

Topic / Unit name	Workload		Mode of delivery	Groups	Collaboration	Feedback	Assessi	ment	
		type					Points	Types	Providers

The Derivative - basic concepts, techniques and rules

Explain the concept of the derivative of a real function of one real variable and its geometric interpretation (90%), Apply differential calculus to find local extrema of a function with one variable and inflection points of the function. (30%), Analyze an elementary function using derivatives and sketch its graph (20%), Define elementary functions of a real variable, analyze their properties and sketch their graphs. (10%)

Concept and definition of the derivative

Introduction of problems - motivation FC approach Video on problems that lead to the derivative: the slope of a tangent, velocity, optimization	30 min	Acquisition	Online	Asynchronous	Teacher not present	No	No	No	No		
Disscusion Students participate in discussions related to the introductory video.	30 min	Discussion	Online	Asynchronous	Teacher not present	No	No	Peer	0	Summative	Peer

Lecture - concept of derivative Professors work with students in a hybrid format on the development od the concept of the derivative, geometric interpretation and definition.	60 min	Acquisition	Hybrid	Synchronous	Teacher	No	No	No	No		
Quiz Students take a short quiz based on the concept od the derivative.	20 min	Assessment	Online	Asynchronous	Teacher	No	No	Automated	1	Summative	Automated
Practice Assistants work with students on derivatives; techniques and rules application.	90 min	Practice	Onsite	Synchronous	Teacher present	No	Yes	Teacher	No		

Independent practical work. Students practice different differentiation techniques based on material in LMS and texbooks.	90 min	Practice	Onsite	Asynchronous	Teacher not present	No	No	Automated	No
Total unit workload	5.33h								
Derivatives of i	mplicit fur	nctions, chair	n rule, h	nigher-order d	lerivative	es			
Video lecture - advanced techniques Students listen to a short video on the introduction advanced techniques of differentiation and then participate in a face to face presentation by the teacher on these	60 min	Acquisition	Hybrid	Synchronous	Teacher	No	No	No	No

techniques.

Quiz Students take a short quiz based on advanced techniques of differentiation.	20 min	Assessment	Online	Asynchronous	Teacher present	No	No	No	2	Summative	Automated
Practice Assistants work with students on examples of derivation of implicit functions and chain rule.	90 min	Practice	Onsite	Synchronous	Teacher present	No	Yes	Teacher	No		
Independent practical work - advanced techniques. Students learn and practice higher-order derivatives based on material in LMS and texbooks.	90 min	Practice	Onsite	Asynchronous	Teacher not present	No	No	Automated	No		

Independent investigation Students are required to investigate on their own the application areas and history of calculus.	90 min	Investigation	Online	Asynchronous	Teacher not present	No	No	No	No
Total unit workload	5.83h								

Topic / Unit name	Workload		Mode of delivery	Groups	Collaboration	Feedback	Assessi	ment	
		type					Points	Types	Providers

Application of derivatives

Apply differential calculus to find local extrema of a function with one variable and inflection points of the function. (60%), Analyze an elementary function using derivatives and sketch its graph (50%), Analyze and solve a problem task in the area of mathematical analysis of the function of one variables (10%)

Finding local extrema

Video-lecture - function extrema Student listen video lecture about finding the absolute (or global) minimum and maximum values of a function.	30 min	Acquisition	Online	Synchronous	Teacher not present	No	No	Teacher	No		
Quiz Students take a short quiz based on finding extrema of function.	20 min	Assessment	Online	Asynchronous	Teacher present	No	No	Automated	1	Summative	Automated

Practice Assistants work with students on finding function increasing or decrease intervals by use of local extrema.	90 min	Practice	Onsite	Synchronous	Teacher	No	Yes	Teacher	No
Independent practical work-finding extrema Students practice finding increasing or decreasing intervals based on material in LMS and texbooks.	90 min	Practice	Onsite	Asynchronous	Teacher not present	No	No	Automated	No

Self- assessment Students take self- assessment based on the assessment tasks in LMS (database). Based on the results they are instructed to further investigate.	90 min	Investigation	Online	Asynchronous	Teacher not present	No	Yes	Teacher	0	Summative	Teacher
Total unit workload	5.33h										
Plotting graph											
Reading- graph plotting Students read material about applying derivatives on plotting graph functions.	60 min	Acquisition	Online	Synchronous	Teacher not present	No	No	No	0	Summative	Automated

Independent practical work - graph plotting Students practice graph plotting based on material in LMS and texbooks.	90 min	Practice	Onsite	Asynchronous	Teacher not present	No	No	Automated	No		
Practice Assistants work with students on plotting graphs.	90 min	Practice	Onsite	Synchronous	Teacher present	No	Yes	Teacher	No		
Self- assessment Students in small group take self- assessment based on the assessment tasks in LMS (database).	90 min	Assessment	Online	Asynchronous	Teacher not present	Yes	Yes	Teacher, Automated	2	Summative	Teacher
Total unit workload	5.5h	_									

Curvature- Concavity and convexity

Video-lecture- Concavity and convexity Student watch video lecture that explains points of inflection, and concavity and convexity of a function.	25 min	Acquisition	Online	Synchronous	Teacher not present	No	No	Teacher	No		
Independent practical work -concavity and convexity Students practice finding point of inflection based on material in LMS and texbooks.	90 min	Practice	Onsite	Asynchronous	Teacher not present	No	No	Automated	No		
Quiz Students take a short quiz about function concavity and convexity.	20 min	Assessment	Online	Asynchronous	Teacher present	No	No	Automated	2	Summative	Automated

Practice Assistants work with students on describing the shape or curvature of a curve.	90 min	Practice	Onsite	Synchronous	Teacher present	No	Yes	Teacher	No		
Self- assessment Students take self- assessment based on the assessment tasks in LMS (database). Based on the results they are instructed to further investigate.	90 min	Investigation	Online	Asynchronous	Teacher not present	No	Yes	Teacher	0	Summative	Teacher
Total unit workload	5.25h										

Topic	/ Unit name	Workload		Mode of delivery	Groups	Collaboration	Feedback	Assessment		
			type					Points	Types	Providers

Monthly test 2

Explain the concept of the derivative of a real function of one real variable and its geometric interpretation (10%), Apply differential calculus to find local extrema of a function with one variable and inflection points of the function. (10%), Analyze an elementary function using derivatives and sketch its graph (20%)

Preparation fot the test

Independent practical work Students work independently	200 min	Practice	Onsite	Asynchronous	Teacher not present	No	Yes	Automated, Peer	No
Disscussion about technical and content related isssues Students are given information in LMS and then they can ask questions.	60 min	Discussion	Online	Asynchronous	Teacher not present	No	Yes	Teacher, Peer	No

Total unit 4.33h workload

Monthly test (kolokvij)

Test The test is	90 min	Assessment	Hybrid	Synchronous	Teacher present	No	No	Teacher, Automated	20	Formative	Teacher, Automated
prepared in											
hybrid delivery											
mode using											
individualised											
assignments											
from the											
databases in											
LMS.											
Total unit	1.5h										

Analysis of the test

workload

Students' feedback A questionnaire with open and closed questions is used. Students give feedback to teachers (technical and content wise).	20 min	Discussion	Online	Asynchronous	Teacher not present	No	No	No	No
Analysis of the test Reliability, validity, students' satisfaction survey, explaining solutions	45 min	Discussion	Hybrid	Synchronous	Teacher present	No	No	Teacher	No

Further student investigation	90 min	Investigation	Online	Asynchronous	Teacher not	Yes	Yes	Peer	No
Students investigate application areas of mathematics learned.					present				
Total unit workload	2.58h								

Topic / Unit name	Workload		Mode of delivery	Groups	Collaboration	Feedback	Assessment			
		type					Points	Types	Providers	

Project team work - PEER ASSESSMENT

Analyze and solve a problem task in the area of mathematical analysis of the function of one variables (5%), Create a program solution for a specific mathematical problem and present the solution in written format (100%)

Preparation for the project

Presentation of teamwork	45 min	Discussion	Hybrid	Synchronous	Teacher present	No	No	No	No
Professors and									
assistants									
present the way									
of working on									
the project, the									
choice of the									
project topic and									
the formation of									
the project team.									
The link of the									
project									
assignment									
(PBL) with the									
learning									
outcomes is									
explained, and									
how the PBL will									
contribute to									
students' future									
jobs. Teachers									
present the									
initial proposal of									
evaluation									
criteria for the									
project. The									

initial criteria				
include: research				
on the				
theoretical				
background,				
investigation of				
possible				
methodology for				
a solution,				
problem				
solution,				
presentation of				
the solution,				
quality of				
teamwork.				
Number of				
students: cca				
100, 3-4 per				
team				

Choice of project topic and team Students form teams of 3-4 (based on their own choice) and then choose a project topic from the list. Students investigate the research topics before making a final choice. Each team will be provided with their own virtual environment for teamwork (wiki).	75 min	Discussion	Online	Asynchronous	Teacher not present	Yes	Yes	No	No
Initial research, discussion and questions Students research the project topic and discuss the topic within the team, but can also ask questions in a discussion forum in the LMS.	90 min	Investigation	Online	Asynchronous	Teacher not present	Yes	Yes	Teacher, Peer	No
Total unit workload Work on project	3.5h								

Disscusion of peer-assessment	45 min	Discussion	Hybrid	Synchronous	Teacher present	No	No	No	No
criteria									
Teachers and									
students discuss									
the criteria for									
project									
assessment, the									
level of									
achievement,									
and how to									
recognize the									
level of									
achievement. At									
the end, a rubric									
is finalized and									
hopefully									
understood by all									
the students.									
The initial									
criteria may be									
changed based									
on discussion.									
The levels of									
achievement will									
be described,									
ranging from 0									
do 4 (depending									
on a specific									
criterion - some									
may have 2, and									
other 3 or 4									
levels).									

Excercise peer- assessment	90 min	Practice	Online	Asynchronous	Teacher present	No	Yes	Teacher, Automated,	No
(peer-grading)								Peer	
Students are									
supposed to									
peer-assess two									
projects (for									
previous years -									
including one									
better and one									
not-so-good) to									
practice how to									
use the LMS,									
criteria, and									
rubrics. After									
that, discussion									
about the									
process is									
performed and									
the criteria are									
clarified if									
necessary.									
Students discuss									
(mutually and									
with the teacher)									
the issues									
related to									
academic									
integrity, fair									
assessment and									
ethical issues									
related to									
cheating.									

Project work	640 min	Production	Hybrid	Asynchronous		Yes	Yes	Teacher,	No
Students					not			Peer	
research the					present				
chosen topic and									
collaborate									
within their									
teams. Students									
solve a project									
task, create a									
software solution									
and/or use									
adequate tools,									
and prepare									
written									
material(s) and									
other necessary									
documentation.									
Finally, they									
upload all the									
artifacts into the									
LMS (workshop									
in Moodle).									
Total unit	12.91h								

Presentation Students' teams present their projects to teachers and other students. Teachers and other students ask questions and discuss the solutions.	120 min	Discussion	Hybrid	Synchronous	Teacher present	Yes	Yes	Teacher, Peer	No		
Assessment and peer-assessment (peer-grading) Students participate in peer-assessment based on the pre-defined assessment criteria and levels of achievement given in the assessment rubric in the Moodle workshop. Each student is assigned with 2 projects to assess - the distribution is done automatically in the Moodle	90 min	Assessment	Hybrid	Asynchronous	Teacher present	No	No	Teacher, Peer	20	Formative	Teacher, Peer

assessment is				
double-blinded:				
students are not				
given				
information				
about whose				
work they are				
assessing or who				
is assessing their				
work. The final				
grade is				
calculated based				
on teacher				
assessment				
(higher weight)				
and student				
peer-assessment				
(lower weight).				
Students are				
given grades for				
(1) their project				
submission and				
(2) their peer-				
assessment.				

Reflection on results	90 min	Investigation	Hybrid	Synchronous	Teacher present	No	Yes	Teacher, Automated,	No
Students and								Peer	
teachers discuss									
the results of the									
PBL and peer-									
assessment,									
based on the									
learning									
analytics									
provided in									
Moodle and not									
on an individual									
basis. Each team									
has the									
opportunity to									
propose									
improvements to									
their artifact									
based on the									
feedback									
received.									
Improved									
artifacts can be									
resubmitted and									
teachers decides									
on whether the									
grades should be									
modified based									
on that.									
on that.									
Total unit	5h								
workload									

Topic / Unit name	Workload		Mode of delivery	Groups	Collaboration	Feedback	Assessi	ment	
		type					Points	Types	Providers

Integration - basic concepts, techniques and rules

Explain the concept of primitive function and integrals of a function with one variable (45%), Determine the primitive function and apply integral calculus in calculating surface area and volume. (20%), Analyze and solve a problem task in the area of mathematical analysis of the function of one variables (35%)

Concept and definition of integration

Introduction of problems - motivation Video on problems that lead to the integral: calculating surface of area, concept of primitive function and integrals of a function (upper and lower Darboux sum).	30 min	Acquisition	Online	Asynchronous	Teacher not present	No	No	No	No		
Disscusion Students participate in discussions related to the introductory video	15 min	Discussion	Online	Asynchronous	Teacher not present	No	No	Peer	0	Summative	Peer

Lecture - concept of integral Professors work with students in a hybrid format on the development od the concept of the integral, geometric interpretation and definition.	120 min	Acquisition	Hybrid	Synchronous	Teacher	No	No	No	No		
Quiz Students take a short quiz based on the concept od the integral	10 min	Assessment	Online	Asynchronous	Teacher present	No	No	Automated	1	Summative	Automated
Total unit workload	2.91h										
Integration tech	niques										
Lecture - advanced techniques Professor presents advanced techniques of integration. Students can ask questions.	90 min	Acquisition	Hybrid	Synchronous	Teacher present	No	No	No	No		

Practice Assistants work with students on integrals; techniques and rules application.	120 min	Practice	Onsite	Synchronous	Teacher present	No	Yes	Teacher	No		
Independent practical work. Students learn and practice bsed on material in LMS and texbooks.	120 min	Practice	Onsite	Asynchronous	Teacher not present	No	No	Automated	No		
Quiz (Integration- math problems) Students take a short quiz based on the concept od the derivative.	30 min	Assessment	Online	Asynchronous	Teacher present	No	No	Automated	2	Summative	Automated
Total unit workload	6h										

Topic / Unit name Wor		Mode of delivery	Groups	Collaboration	Feedback	Assessment			
	type					Points	Types	Providers	

Application of integral calculus

Explain the concept of primitive function and integrals of a function with one variable (35%), Determine the primitive function and apply integral calculus in calculating surface area and volume. (60%)

Calculating surface area

Lecture - calculating surface Student listen video lecture about calculating surface area.	45 min	Acquisition	Online	Synchronous	Teacher not present	No	No	Teacher	No		
Quiz Students take a short quiz based on calculating surface area.	20 min	Assessment	Online	Asynchronous	Teacher present	No	No	Automated	1	Summative	Automated

Lecture Professor	120 min	Acquisition	Hybrid	Synchronous	Teacher present	No	No	No	No
checks how									
many students									
watched the									
video lesson									
and what the									
quiz results									
were. Based on									
the results of									
the quiz,									
teacher repeats									
concepts that									
are less well									
understood and									
designs lecture									
to upgrade and									
broad the topic.									
Students have									
possibility for									
additional									
questions.									
Practice Assistants work with students on calculating surface area.	120 min	Practice	Onsite	Synchronous	Teacher present	No	Yes	Teacher	No
Independent practical work-calculating surface area Students practice calculating surface area.	180 min	Practice	Onsite	Asynchronous	Teacher not present	No	No	Automated	No

Self- assessment Students take self- assessment based on the assessment tasks in LMS (database).	90 min	Assessment	Online	Asynchronous	Teacher not present	No	Yes	Teacher	2	Summative	Teacher
Total unit workload	9.58h										
Calculating volu	me										
Lecture - calculating volume Student listen video lecture about calculating volume.	30 min	Acquisition	Online	Synchronous	Teacher not present	No	No	Teacher	No		
Quiz Students take a short quiz based on calculating	20 min	Assessment	Online	Asynchronous	Teacher present	No	No	Automated	1	Summative	Automated

volume.

Lecture Professor	90 min	Acquisition	Hybrid	Synchronous	Teacher present	No	No	No	No
checks how									
many students									
watched the									
video lesson									
and what the									
quiz results									
were. Based on									
the results of									
the quiz,									
teacher repeats									
concepts that									
are less well									
understood and									
designs lecture									
to upgrade and									
broad the topic.									
Students have									
possibility for									
additional									
questions.									
Practice Assistants work with students on calculating volume.	90 min	Practice	Onsite	Synchronous	Teacher present	No	Yes	Teacher	No
	120 '	B	0 ''						
Independent practical work- calculating volume	120 min	Practice	Onsite	Asynchronous	Teacher not present	No	No	Automated	No
Students									
practice									
calculating									
volume.									
volulle.									

Self- assessment Students take self- assessment based on the assessment tasks in LMS (database).	90 min	Assessment	Online	Asynchronous	Teacher not present	No	Yes	Teacher	2	Summative	Teacher
Total unit workload	7.33h										

oic / Unit name	Workload		Mode of	f delivery		Groups	Collaboration	Feedback	Assessment		
		type					Points	Types	Providers		
onthly test	3										
olain the concep	t of primitiv	e function and	integrals	of a function wi	th one var	iable (20 '	%), Determine	the primitive f	unction a	and apply i	integral
culus in calculat	ing surface	area and volur	ne. (20 %)							
onaration fot	the test										
eparation fot	the test										
Independent	200 min	Practice	Onsite	Asynchronous	Teacher	No	Yes	Automated,	No		
practical work Students work					not present			Peer			
independently					P						
Disscussion	60 min	Discussion	Online	Asynchronous	Teacher	No	Yes	Teacher,	No		
about technical					not			Peer			
and content related isssues					present						
Students are											
given											
nformation in											
mormacion in											
LMS and then they can ask											

Total unit 4.33h workload

Monthly test (kolokvij)

Test The test is	90 min	Assessment	Hybrid	Synchronous	Teacher present	No	No	Teacher, Automated	20	Formative	Teacher, Automated
prepared in											
hybrid delivery											
mode using											
individualised											
assignments											
from the											
databases in											
LMS.											
Total unit	1.5h										

Analysis of the test

workload

Students' feedback A questionnaire with open and closed questions is used. Students give feedback to teachers (technical and content wise).	20 min	Discussion	Online	Asynchronous	Teacher not present	No	No	No	No
Analysis of the test Reliability, validity, students' satisfaction survey, explaining solutions	45 min	Discussion	Hybrid	Synchronous	Teacher present	No	No	Teacher	No

Further student investigation	90 min	Investigation	Online	Asynchronous	Teacher not	Yes	Yes	Peer	No
Students investigate application areas of mathematics learned.					present				
Total unit workload	2.58h								

Total course workload: 138.66h